# Quantum Mechanical Calculation of Stability in 2-Formyl N-Methyl Pyridinium (Cation) Oxime (2-PAM<sup>+</sup>) Conformers

WALLY GIORDANO, JON R. HAMANN, JEROME J. HARKINS, AND JOYCE J. KAUFMAN

Medical Research Laboratory, USAEARL, Edgewood Arsenal, Maryland; Chemistry Department, New York University, Washington Square, New York, New York; Physics Department, Research Institute for Advanced Studies (RIAS), Martin Company, Baltimore, Maryland

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# SUMMARY

- 1. Twelve conformers of 2-formyl N-methyl pyridinium (cation) oxime (2-PAM<sup>+</sup>) were geometrically defined and were subjected to extended Hückel molecular orbital (XHMO) quantum mechanical calculation.
- 2. The parameter molecular total overlap population (MTOP) was described and was shown to reflect stability and, in this study, to predict expected geometry.
- 3. By analyzing total energy (TE) and molecular total overlap population (MTOP), within the limitations of the conditions used and the validity of the approximations in the model chosen, the least stable isomers were found to be the two planar oxime-trans pairs ( $N_1T_-$  and  $N_3T_-$ ); the most stable planar isomers were found to be those with oxime syn (cis), and of these the proton pair with aldoxime nitrogen vicinal to ring three ( $N_3S_-$ ) was found to be slightly more stable than its ring counterpart ( $N_1S_-$ ); the most stable of all conformers were found to be the aldoxime out of plane (OOP) quartet; for any rotational state the syn (cis) oxime configuration was found to be more stable than its respective anti (trans) analog; for any nonsterically hindered aldoxime-ring rotational and oxime configurational state the proton sun (cis) analog.
- 4. By evaluating differences in the same parameters used above, barriers to rotation, conformation, and configuration were estimated and the energetic implications suggested were deemed significant to consider that the most stable conformers are likely to retain their identity at room temperature in slightly acidic solution (their protonated states).
- 5. The feasibility, implicit in an earlier study, of theoretically determining conformational stability, barriers to rotation, conformation, and configurational stereoisomerism of molecules in the free molecular state (and possibly in dilute solution) is partially and tentatively substantiated.
- 6. Although by using total energy (TE) alone, the expected geometry was not predictable from the three aldoxime-ring bond lengths chosen, molecular total overlap populations (MTOP's) clearly indicated that maximal stability should occur between 1.40 Å and 1.55 Å for planar conformers and very close to 1.55 Å for OOP conformers. This finding may generally imply that any molecule can have its exact geometry accurately predicted by theoretical calculations alone.
- 7. The use of structures derived from crystallography in the stereochemical and quantum chemical analysis of chemical reactivity in solution is suggested at least at times to be precarious.

# INTRODUCTION

In 1957, the chemical synthesis of the methiodide of 2-pyridine aldoxime PAM-I) was reported (1). Two forms were described in which the more stable, higher melting point, yellow solid was tentatively identified on chemical arguments as having the anti configuration. This so-called B form had been tested in enzyme reactivation studies and in organophosphorus-intoxicated animals and had been found to exhibit exceptional activity (2). In 1958, considering the analogy with neostigmine, it was argued on the basis of molecular complementarity that 2-PAM-I was planar and in an anti configuration with the oxygen close to the 3 position in the pyridinium ring (3).

In 1961, by chemical and UV analysis, the unstable A form was designated a carbinolamine rather than an oxime (4). A year later this same group examining NMR data of stable 4-PAM-I concluded it was in the syn configuration and suggested the instability of the anti stereoisomer (5). In 1964, by base catalyzed degradation—UV studies, the A isomer was reported to be most likely a mixture of carbinolamine and anti oxime whereas the B isomer was syn (6).

In an analysis previously reported this year as the first of a series of theoretical treatises on the stereochemical and quantum chemical considerations of the same pyridine aldoximes, the basis for evaluating multiple stereochemical states of 2-PAM was laid. At that time it was argued that as a start the exact conformation, including rotations about the ring-aldoxime bond, and syn-anti configurations of the oxime as well as the oxime proton, had to be included in a thorough, although not exhaustive, quantum mechanical evaluation. It was noted that inasmuch as crystallography of the solid state does not necessarily describe the state in solution and that, since X-ray analysis of solutes is not practical nor have other powerful physical tools been capable of defining the

<sup>1</sup> W. Giordano and J. R. Hamann. Submitted to J. Pharm. Sci.

exact stereochemistry or quantum chemistry, a theoretical approach was both timely and necessary (7).

With the problem thus defined, the following initial study was undertaken (7). The rotameric states of 2-PAM were categorized and subjected to the most modern and appropriate semiempirical quantum mechanical calculation known (8). The ensuing energetics, their implications and limitations, were analyzed.

# METHODOLOGY AND GEOMETRY

- A. The extended Hückel molecular orbital (XHMO) calculation has been described previously (8). Essentially, for this initial study the following conditions were used:
- 1. The 52 valence shell electrons alone were treated without explicit inclusion of electron-electron interaction or nuclear-nuclear interaction. The molecule was thus assumed to be formally positive.
- 2. The basis set consisted of Slater type orbitals (STO) with shielding coefficients  $(\mu)$  as described previously (see, e.g., ref. 9)

$$X_{STO}(r,\theta,\phi) = Nr^{n-1} \exp(-\mu r) Y_l^m(\theta,\phi)$$

where N is a normalizing constant. The  $X_{STO}$  for pyridinium nitrogen was chosen as that having a four electron valance state.

- 3. The overlap integrals  $(S_{11})$  between these STO's were calculated as described by Mulliken *et al.* (10). The pyridinium nitrogen was assigned four electrons for this calculation.
- 4. The one-center integrals making up the diagonal elements of the Hamiltonian matrix  $(H_{11})$  were set equal to the appropriate valence state ionization potentials (VSIP) (11, 12) [see Table 1]. The VSIP of the pyridinium nitrogen was chosen as that of the neutral state.
- 5. The resonance integrals or nondiagonal elements  $(H_{11})$  of the Hamiltonian matrix were constructed according to the following formula (13):

$$H_{ii} = 0.5(H_{ii} + H_{ii})S_{ii}(2 - |S_{ii}|)$$

TABLE 1
Valence state ionization potentials (VSIP) used as

diagonal elements (H<sub>ii</sub>) in the Hamiltonian matrix

These values were chosen from values previously

These values were chosen from values previously derived (12). Nitrogen used was that in the neutral valence state.

Atom	Atomic orbital	Valence state ionization potentials (VSIP) (electron volts)
Н	18	-13.60
c	2S	-19.52
_	<b>2P</b>	-9.75
N	2S	-25.58
	<b>2P</b>	-12.38
0	<b>2</b> S	-32.30
	2P	-14.61

It should be noted that special attention must be given formulas of this type in order to minimize the effects of transformational non-invariances.

B. The input geometry consisted of 12 conformers in which the following arbitrary

numbering system and assignment of positions and designations was made. A conformer with the aldoxime nitrogen planar and vicinal to carbon three (ring) is designated N<sub>3</sub> (see Fig. 1). Likewise N<sub>1</sub> implies that this nitrogen is planar and vicinal to the pyridinium nitrogen (ring). A 90-degree rotation of the aldoxime nitrogen in either direction from any planar position is an equivalent position and puts the nitrogen a maximum distance from the plane of the ring. The designation used was N↑. This was the only out-of-plane nitrogen position studied and was chosen to most likely demonstrate the effect of this rotation. Other out of plane (OOP) positions are reserved for later studies. For each of the above positions the aldoxime oxygen was set either syn (same side) or anti (opposite side) with respect to the aldoxime carbon's proton (H<sub>7</sub>) and designated O<sub>s</sub> or O<sub>t</sub>, respectively (see Fig. 1). Likewise the aldoxime oxygen's proton (H<sub>n</sub>) was set on the same side (syn or cis) or opposite side (anti or trans)

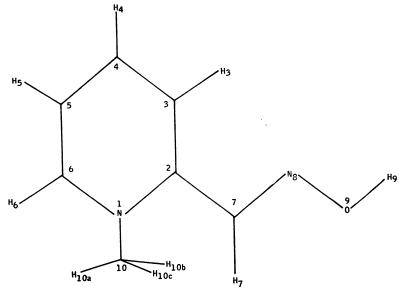


Fig. 1. Numbering and name convention for 2-formyl N-methyl pyridinium (cation) oxime (2- $PAM^+$ ),  $N_*O_*H_* = N_*SS$  conformer

Purely arbitrary except ring nitrogen and carbon. Atoms in conformer designation refer to those in the aldoxime side chain. N<sub>s</sub> refers to aldoxime nitrogen vicinal to ring 3 position and in the same plane. O<sub>s</sub> refers to aldoxime oxygen syn (cis) to proton of aldoxime carbon (standard American Chemical Society nomenclature). H<sub>s</sub> refers to aldoxime hydroxyl proton syn (cis) to aldoxime nitrogen lone pair electrons (purely arbitrary).



Mol. Pharmacol. 3, 307-317 (1967)

TABLE 2
Bond lengths in angstroms versus bond types
Choice was based on expected values from crystallographic studies (14-16) and footnote 2.

Bond type	Bond length (Å)
Ring C—C or C—N	1.40
C—H (all)	1.08
$C_{7}-N_{8}$	1.26
N <sub>8</sub> O <sub>9</sub>	1.39
O <sub>9</sub> —H <sub>9</sub>	0.97
N <sub>1</sub> —C <sub>10</sub>	1.45
	(1.40 Set I
C <sub>2</sub> —C <sub>7</sub>	$\{1.55 \text{ Set II}\}$
	(1.70 Set III

with respect to the aldoxime nitrogen lone pair and designated H<sub>s</sub> or H<sub>t</sub> respectively (see Fig. 1). Three sets were designated according to the bond length between carbon 2 and carbon 7. Table 2 contains these bond lengths as well as the lengths

(15, 16). These bond lengths are not to be construed as anything more than a reasonable starting point, and the same point is to be made concerning the bond angles, which were all set equal to 120 degrees. It is further noted that this initial study is concerned solely with the protonated or acidic state of the cation (no anion included).

#### RESULTS

# A. Total Energy

The total energy, which is in fact the internal (ground state) energy of a single molecule at zero degrees and under no external perturbations, is here expressed in electron volts (eV), where 1 eV = 23.061 kilocalories (kcal). Table 3 contains the total energies (all have negative sign) for each of the twelve conformers in each of the three sets. The larger the negativity

Table 3

Total energies for each conformer at each  $C_2$ — $C_7$  bond length

Total energy (electronic), at zero degrees, of the ground state of a single conformeric molecule in electron volts (the greater the negativity the greater the stability). See text and Fig. 1 for conformeric designations.

Conformer	Bond length, $C_2$ — $C_7$ (Å)		
	1 .40 I	1.55 II	1.70 III
N↑TT	-858.84131	-859.79601	-860.38558
N TS	-858.67233	-859.61012	-860.18550
N ↑ ST	-858.85130	-859.73120	-860.09119
N ↑ SS	-858.68282	-859.56560	-859.91885
N <sub>2</sub> TT	-852.58314	-854.43677	-855.77232
N <sub>2</sub> TS	-853.71936	-855.59515	-856.77740
N <sub>2</sub> ST	-856.79145	-857.85085	-858.47557
N <sub>2</sub> SS	-856.94263	-857.99878	-858.63718
$N_1TT$	-849.67167	-848.58391	-847.90159
$N_1TS$	-844.02016	-846.59140	-848.16136
$N_1ST$	-855.93046	-857.28247	-858.01933
Niss	-855.33867	-856.69140	-857.42384

used for all the other bonds throughout this group of calculations. These lengths were chosen by reviewing general tabulations of crystallographic data (14) as well as the extensive list of published and unpublished<sup>2</sup> crystal structures of aldoximes the more stable the molecule. The absolute magnitude of the total energy is not to be considered sufficiently accurate, since the model has not yet been quantitatively parameterized, for comparison with heats of formation as empirically measured, but the relative order should be a fair, but not necessarily an unequivocal indication of

<sup>&</sup>lt;sup>2</sup>B. Jerslev, private communication.

stability. Clearly indicated is the marked instability of the  $N_1TT$  and  $N_1TS$  conformers in all sets. The  $N_3TT$  and  $N_3TS$  conformers likewise are less stable, but begin to show significant gain in their stability with increasing  $C_2$ — $C_7$  bond

the calculations indicate that the out of plane conformers (OOP) are significantly more stable than any planar isomer, including the  $N_3S$  pair. The most stable of the out of plane conformers is  $N \uparrow TT$ , and the  $N \uparrow ST$  conformer is more stable than

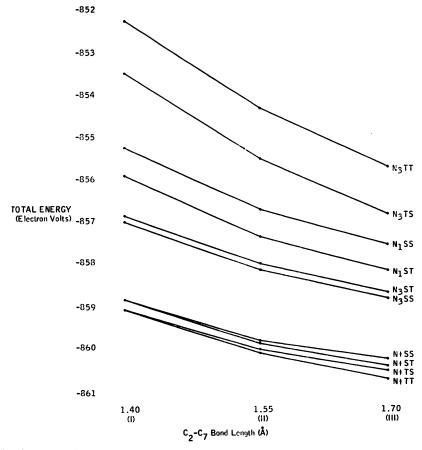


Fig. 2. Total energy of each conformer versus  $C_x$ — $C_1$  bond length

The total energy of each conformer is the energy in electron volts for the ground state of the free molecule at zero degrees Kelvin calculated according to the method described in the text. The greater the negativity, the greater the stability. The calculations were made for each conformer at three C<sub>2</sub>—C<sub>1</sub> bond lengths (Angstroms) 1.40 (Set I); 1.55 (Set II), 1.70 (Set III). For atom numbering and conformer designation see Fig. 1 and text. The connecting lines are used only for convenience in following each conformer and are not to be considered an energy surface. Conformers N<sub>1</sub>TT and N<sub>1</sub>TS are so unstable they are off (above) this scale.

length. The planar syn (cis) conformers are always significantly more stable than the planar anti (trans) conformers. The  $N_sS$  pair are the most stable planar conformers in all sets, but less significantly so when compared to the  $N_1S$  pair at the longer  $C_2$ — $C_7$  bond lengths. In every set,

both its proton syn isomer or  $N \uparrow TS$ . The  $H_t$ 's in the  $N_1$  category are generally more stable than their proton syn isomers while the reverse prevails throughout the  $N_3$  category. Looking at Fig. 2 as well as Table 3, it is to be noted that all conformers with the exception of  $N_1TT$  get

appreciably more stable as the  $C_2$ — $C_7$  bond length is increased from 1.40 Å to 1.70 Å.

# B. Molecular Total Overlap Population (MTOP)

The electron density between any two atoms i and j, whether bonded or non-bonded, is represented by the total overlap population (TOP) between these centers. This TOP is related to the binding energy between two atoms. If the TOP between any two atoms is summed over all centers, this molecular total overlap population (MTOP) should be somewhat indicative of the total binding energy of the entire molecule and therefore of its stability. Table 4

TABLE 4
Molecular total overlap populations for each conformer at each C<sub>2</sub>—C<sub>7</sub> bond length

Molecular total overlap population (MTOP) in terms of electron density (probability) (the greater the positivity the greater the stability). See text and Fig. 1 for conformeric designations.

	Bond length, $C_2$ — $C_7$ (Å)			
Conformer	1.40 I	1.55 II	1.70 III	
N↑TT	12.87752	12.87124	12.84096	
N TS	12.88003	12.86991	12.83852	
N ↑ ST	12.89289	12.97777	12.85640	
N ↑ SS	12.88360	13.00684	12.84593	
N.TT	12.02921	12.40763	12.58712	
N <sub>2</sub> TS	12.76276	12.80891	12.81299	
N <sub>2</sub> ST	12.85392	12.85346	12.82614	
N <sub>2</sub> SS	12.85017	12.84785	12.82223	
N <sub>1</sub> TT	5.32280	9.30883	10.84311	
N <sub>1</sub> TS	12.18220	12.26605	12.81952	
NIST	12.82014	12.83448	12.82302	
N <sub>1</sub> SS	12.81282	12.82660	12.81478	

lists the values calculated for each conformer in each set and it is readily noted that the least stable conformer is N<sub>1</sub>TT. It shows marked improvement at longer C<sub>2</sub>—C<sub>7</sub> bond lengths as does N<sub>1</sub>TS to a lesser extent. The latter, in fact, is more stable than N<sub>1</sub>SS and almost as stable as N<sub>1</sub>ST at 1.70 Å. The N<sub>3</sub>TT conformer improves moderately with increasing bond length and N<sub>3</sub>TS does so to a lesser extent.

The N<sub>3</sub>S<sub>-</sub> pair are the most stable planar conformers with the N<sub>1</sub>S<sub>-</sub> pair close behind. Both demonstrate less stability above 1.55 A. The out of plane conformers are clearly more stable than the planar conformers with the N \(\cap\) S\_ pair the most stable of the entire group. The stability of the out of plane conformers falls off at bond lengths greater than 1.55 Å. The most outstanding example of peaking at or near 1.55 Å was demonstrated by the N \(\backslash S\_ pair as can be seen in Fig. 3 and extrapolation of all others except the unstable N<sub>1</sub>T<sub>-</sub> and N<sub>3</sub>T<sub>-</sub> pairs suggest a maximum stability between 1.40 Å and 1.55 Å. Certainly in these "nonsterically hindered" conformers the stability at 1.70 Å is minimal. The proton anti (trans) is generally more stable throughout the group with the obvious exceptions again of the N<sub>1</sub>T<sub>-</sub> and N<sub>3</sub>T<sub>-</sub> pairs. Generally then, the ordering of stabilities mimics that derived from the total energy with the minor exception that the out of plane N \(\cap\)SS and N \(\cap\)TT interchange, as does planar N<sub>3</sub>ST with N<sub>3</sub>SS, and N<sub>1</sub>TS with N<sub>1</sub>TT (both being oxime proton configurational changes).

# C. Rotational Barriers and Conformational Analysis

By taking the differences in total energy or MTOP between any two conformers, the magnitude of the barrier to rotation or conversion from one conformer to any other can be estimated. Tables 5-8 contain compilations of these values. As can be seen from Table 5, the range of the barrier to rotation from the out of plane state to the planar state is smaller for syn (cis) conformers (1.28-3.30 eV) than for anti (trans) conformers (3.41-14.65 eV). Generally the conversions are smaller at the longer bond lengths. The conversion to N↑SS from N<sub>3</sub>SS at 1.70 Å is the smallest energy change in the entire series, and at 1.28 eV is equivalent to 29.44 kcal. Examination of MTOP differences in Table 6 reveal that the largest conversions for hydroxyl syn (cis) isomers are at 1.55 Å, but in all other respects the trends follow the energy analysis. The energy differences expected from hydroxyl syn

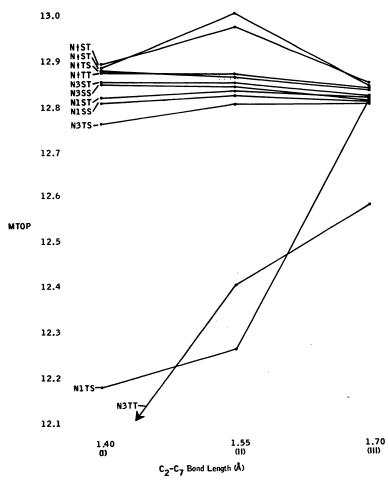


Fig. 3. Molecular total overlap population (MTOP) for each conformer versus  $C_{2}$ — $C_{1}$  bond length. The molecular total overlap population of each conformer is the sum of the overlap populations between each atom and every other atom expressed in terms of density (probability) of electrons and calculated according to the method described in the fext for the ground state of the free molecule at zero degrees Kelvin. The greater the positivity the greater the stability. The calculations were made for each conformer at three  $C_{2}$ — $C_{1}$  bond lengths (Angstroms): 1.40 (Set I); 1.55 (Set II); 1.70 (Set III). For atom numbering and conformer designation see Fig. 1 and text. The connecting lines are used only for convenience in following each conformer and are not to be considered a stability-equivalent surface. Conformer  $N_{1}TT$  and Set I of conformer  $N_{1}TT$  are so unstable they are off (below) this scale.

(cis)-anti (trans) configurational conversion as seen in Table 7 are all positive for planar conformers and mixed for out of plane conformers. Here, where a positive sign implies an energy cost (i.e., less stability), the range in the planar conformers is much larger on the basis of the great instability of the anti (trans) conformers. Differences within the OOP conformers are small enough to be randomized

by thermal effects. In striking contrast, the differences for the same conversions as measured by MTOP in Table 8 are all negative, indicating the greater stability of the syn (cis) conformers in any rotational and proton configurational state.

# DISCUSSION

In the XHMO model the total energy is obtained as the sum over the orbital en-

Table 5

Total energy (TE) change in converting (rotating) a planar conformer to its OOP analog at its respective  $C_2$ — $C_7$  bond length

Total energy (electronic), at zero degrees, of the ground state of a single conformeric molecule in electron volts (the greater the negativity the greater the stability). See text and Fig. 1 for conformeric designations. Negative values imply a total energy gain (more stable) due to the conversion.

	Bond length, C <sub>2</sub> —C <sub>7</sub> (Å)		
G	1.40	1.55	1.70
Conversion	1	II	III
To From			
$N \uparrow TT - N_{3}TT$	-6.25815	-5.35924	-4.61326
N↑TS - N.TS	-4.95297	-4.01497	-3.40810
$N \uparrow ST - N_3ST$	-2.05985	-1.88035	-1.61562
N↑SS - N₃SS	-1.74019	-1.56682	-1.28167
$N \uparrow TT - N_1TT$	-9.16964	-11.21210	-12.48399
$N \uparrow TS - N_1 TS$	-14.65217	-13.01872	-12.02414
$N \uparrow ST - N_1ST$	-2.92084	-2.44873	-2.07186
$N \uparrow SS - N_1SS$	-3.34415	-2.87420	-2.49501

ergies of the occupied levels. In that the elements are not yet quantitatively parameterized, the Hamiltonian matrix is not a perfect approximation to the Hartree-Fock Hamiltonian which yields reasonably accurate total energies. Hence the magni-

TABLE 6

Differences in molecular total overlap populations (MTOP) in converting (rotating) any planar conformer to its (out of plane) analog at respective C<sub>2</sub>—C<sub>7</sub> bond lengths

Molecular total overlap population (MTOP) in terms of electron density (probability) (the greater the positivity the greater the stability). See text and Fig. 1 for conformeric designations. Positive values imply a gain in MTOP (greater stability) due to the conversion.

	Bond length, C <sub>2</sub> —C <sub>7</sub> (Å)		
Conversion	1.40 I	1.55 II	1.70 III
To From			
N↑TT - N₁TT	.84831	. <b>46361</b>	.25384
N↑TS - NaTS	.11727	.06100	.02553
$N \uparrow ST - N_2ST$	.03897	.12431	.03026
N TSS - NaSS	.03343	.15899	.02370
$N \uparrow TT - N_1TT$	7.55472	3.56241	1.99785
$N \uparrow TS - N_1 TS$	.69783	.60386	.01900
$N \uparrow ST - N_1ST$	.07275	.14329	.03338
$N \uparrow SS - N_1SS$	.07078	.18024	.03115

tude of the XHMO orbital energies, and consequentially the total energy, is quantitatively undeterminable. Relative differences among the orbital energies as well as

Table 7

Total energy (TE) differences for all conversions of OH from syn (cis) to anti (trans) for each  $C_2$ — $C_1$  bond length

Total energy (electronic), at zero degrees, of the ground state of a single conformeric molecule in electron volts (the greater the negativity the greater the stability). Positive values imply loss in energy (less stability) due to the conversion.

	Bond length, C <sub>2</sub> —C <sub>7</sub> (Å)		
Conversion	1.40 I	1.55 II	1.70 III
To From			<del></del>
$N \uparrow TT - N \uparrow ST$	.00999	06481	<b>29439</b>
$N \uparrow TT - N \uparrow SS$	15849	23041	46653
$N \uparrow TS - N \uparrow ST$	. 17897	.12108	09431
$N \uparrow TS - N \uparrow SS$	.01049	<b>-</b> . <b>04452</b>	<b>-</b> .17234
$N_{2}TT - N_{2}ST$	4.20831	3.41408	2.70325
$N_{2}TT - N_{2}SS$	4.35949	3.56201	2.86486
$N_{2}TS - N_{2}ST$	3.07209	2.25570	1.69811
$N_{2}TS - N_{2}SS$	3.22327	2.40363	1.85978
$N_1TT - N_1ST$	6.25879	8.69856	10.11774
$N_1TT - N_1SS$	5.66700	8.10749	9.52225
$N_1TS - N_1ST$	11.91030	10.69107	9.85797
$N_1TS - N_1SS$	11.31851	10.10000	9.26248

TABLE 8

Molecular total overlap population (MTOP) differences for all conversions of OH from syn (cis) to anti (trans) for each  $C_2$ — $C_1$  bond length

Molecular total overlap population (MTOP) in terms of electron density (probability) (the greater the positivity the greater the stability). Negative values imply loss in MTOP (less stability) due to the conversion.

Conversion	Bond length, $C_T$ — $C_7$ (Å)		
	1.40 I	1.55 II	1.70 III
To From			
$N \uparrow TT - N \uparrow ST$	01537	10653	01544
$N \uparrow TT - N \uparrow SS$	00617	<b>13560</b>	00497
$N \uparrow TS - N \uparrow ST$	01286	<b>10786</b>	01788
$N \uparrow TS - N \uparrow SS$	00357	<b>13693</b>	00741
N <sub>2</sub> TT - N <sub>2</sub> ST	<b>82471</b>	<b>44583</b>	<b>23902</b>
NaTT - NaSS	82096	<b>44022</b>	<b>23511</b>
NaTS - NaST	<b>09116</b>	<b>04455</b>	<b>-</b> . 01315
NaTS - NaSS	<b>08741</b>	03894	<b>-</b> .00924
$N_1TT - N_1ST$	<b>-7.49734</b>	-3.52565	-1.97991
N <sub>1</sub> TT - N <sub>1</sub> SS	-7.49002	-3.51777	-1.97167
$N_1TS - N_1ST$	6379 <del>4</del>	<b>56843</b>	00350
$N_1TS - N_1SS$	<b>63062</b>	<b>56055</b>	<b>-</b> . 00474

among the total energies for comparable systems, however, have been observed to be satisfactory for predictions of electronic transition energies and relative molecular stabilities.

The choice of MTOP as a measure of the stability of a molecular system depends formally upon the validity of the interpretation of the maximum overlap principle, i.e., that physical systems tend to exist in a state characterized by a conditional maximum of the overlap. It has been shown that in the simple Hückel model of homonuclear  $\pi$ -electron systems the solution of the minimum-energy problem is equivalent to the solution of the maximumoverlap problem when  $H_{ij} = K S_{ij}$ . For a heteroatomic system, or when  $H_{ij}$  is not directly proportional to  $S_{ij}$ , as in our XHMO model, the two solutions deviate and the deviation is some measure of the noncommutability of H and S, i.e.,  $HS \neq$ SH (17). It is to be noted that when the two variational principles do not lead to equivalent results it would be expected that the minimum-energy principle is the more valid of the two; however, it is well known that in Hückel models different parameters are necessary for calculating different properties (18). Hence it is possible to have a Hamiltonian matrix which yields better electron distributions (as obtained from a Mulliken wave function analysis) than energies.

Finally, it should be pointed out that the more general validity of the minimum-energy principle is inferred from its relation to the maximum-entropy principle,<sup>3</sup> and from a generalization of a previous perturbation treatment of molecular stability (19). In this latter, the total energy E is written as

$$E = \sum_{i} [(NAP)_{i}H_{ii}] + 2 \sum_{i \neq j} \left[ \frac{(TOP)_{ij}}{S_{ij}} H_{ij} \right]$$

Hence it is seen that the overlap population between orbitals i and j ([TOP]<sub>1j</sub>) enters as one factor among several in the expression for E and MTOP =  $\sum_{i \neq j}$  (TOP)<sub>1j</sub> is not involved explicitly as such.

<sup>2</sup>J. R. Hamann and W. Giordano, submitted to *Theoret. Chim. Acta*.

In accord with this view, it can be observed that MTOP has an extremum as a function of the C<sub>2</sub>—C<sub>7</sub> bond distance which appears within the expected bounds for a C<sub>2</sub>—C<sub>7</sub> bond length in aromatic ring linked aldoximes; however, the total energy exhibits no such extremum. It should be emphasized that this lack of correlation of the energy with optimum bond length applies to the magnitude of the energy and not necessarily to energy differences. In fact, the relative ordering of the total energies generally mimics the ordering of the MTOP's; hence the two methods of estimating relative stabilities are largely mutually consistent.

Assuming then that on theoretical grounds the MTOP analysis can be expected to be a reasonable indication of molecular stability and since the total energy correlation is good, certain observations may be made. To begin with, proton configuration may be a significant perturbation as suggested by these calculations. Certainly this would not be expected for the nonsterically hindered conformers on classical grounds. Secondly, planar anti (trans) conformers should have a very low probability of existence. In fact, some TOP's of certain bonds in N<sub>1</sub>TT were negative, indicative of an antibonding state (7); that is, there would be two fragments and, therefore, no longer a single molecule. Furthermore, although there was indication of C<sub>3</sub>—H<sub>3</sub>———O<sub>3</sub> hydrogen bonding in  $N_3TS$  (7) there is no improvement of the molecular wave function over N<sub>3</sub>SS as demonstrated by MTOP analysis. Third, the markedly greater stability of N<sub>3</sub>S and N<sub>1</sub>S planar conformers in this study has been suggested experimentally by previous work (5, 6). Furthermore, since the syn(cis) out of plane conformers are generally as stable as anti (trans) out of plane conformers the syn (cis) configuration that was reported may in fact be the out of plane syn (cis). Fourth, recent crystallographic analysis of 2-PAM-I (16),2 has demonstrated that the N<sub>3</sub>S conformation prevails in the solid state. The markedly greater stability of the out of plane conformers in the present study, which is a study of the free molecular state and, therefore, slightly more analogous to the state in dilute solution, may be either an indication of a conformeric conversion in changing state from solid to solution or may be attributable to an inadequacy of the theoretical model used in this study.

In favor of the former is the reasonable theoretical foundation of the MTOP analysis and the fact that this study has indicated N<sub>3</sub>S<sub>-</sub> is the most stable planar conformeric pair. Classically, on qualitative and prior empirical grounds, the resonance energy gain in the planar state would be thought sufficient to outweigh the loss, if any, in "nonbonded interactions." In fact, the reverse is what these calculations have implied. It might be added that although "planar" 2-PAM-I solid is yellow, the chloride salt is white, and since both are yellow in basic solution (deprotonated), but colorless in acid (protonated), these observations (20) might be interpreted as a correlation of color with planarity and lack of it with nonplanarity! A crystallographic study of 2-PAM-Cl should help resolve this issue. Recent electron spin resonance spectroscopy of the chemical oxidation intermediates of 2-PAM in aqueous solution has demonstrated two, and at times three, distinct free radical species, one of which suggests an out of plane state.

The adequacy of the XHMO model chosen in this study cannot be established unequivocally by this preliminary work and since it must await additional evaluation now in process the interpretation of results must be spoken of reservedly. If nothing else, a serious question is raised with respect to the relation in general of crystallographic analysis of the solid state of molecules and their structures in solution. The implications that these observations suggest and the considerations that they should provoke must be evaluated for incorporation in future experimental studies and design.

<sup>4</sup> W. Giordano and P. G. Mennitt, unpublished results.

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#### REFERENCES

- S. Ginsberg and I. Wilson, J. Am. Chem. Soc. 79, 481 (1957).
- I. Wilson and S. Ginsberg, Biochim. Biophys. Acta 18, 269 (1955); D. R. Davis and A. L. Green, Discussions Faraday Soc. 20, 269 (1955)
- I. Wilson, in "Elementary Processes of Nerve Conduction and Muscle Contraction" (D. Nachmanson, ed.), p. 163. Academic Press, New York, 1960.
- E. Poziomek, D. Dramer, B. Fromm and W. Mosher, J. Org. Chem. 26, 423 (1961).
- E. Poziomek, D. Dramer, W. Mosher and H. Michel, J. Am. Chem. Soc. 83, 3916 (1961).
- R. Ellin and J. Wills, J. Pharm. Sci. 53, 995 (1964).
- W. Giordano, J. R. Hamann, J. J. Harkins and J. J. Kaufman in "Physical-chemical

- Aspects of Drug Action" (E. J. Ariëns, ed.), in press.
- M. Wolfsberg and L. Helmholz, J. Chem. Phys. 20, 837 (1952); R. Hoffman, J. Chem. Phys. 39, 1397 (1963).
- H. Eyring, J. Walter and G. E. Kimball, "Quantum Chemistry" p. 163. Wiley, New York, 1944.
- R. S. Mulliken, C. A. Riecke, D. Orloff and H. Orloff, J. Chem. Phys. 17, 1248 (1949).
- J. Hinze and H. H. Jaffe, J. Am. Chem. Soc. 84, 540 (1962).
- F. F. Mortimer et al., Shell Development Company Technical Reports, Contract DA 31-124-ARO(D)-54 (Dec. 1962 et. seq.).
- L. C. Cusacks, Presented at Conference in Quantum Mechanics, Sannabel Island, Florida, January 1964, and p. 36 of Rept. No. 50 Quantum Theory Project, Univ. of Florida, Gainsville, Florida.
- L. E. Sutton, Chem. Soc. (London) Special Publ. 11 (1958).
- K. Folting, W. N. Lipscomb and B. Jerslev, *Acta Cryst.* 17, 1263 (1964).
- 16. D. Carlstrom, Acta Chem. Scand. in press.
- P. G. Lykos and H. N. Schmeising, J. Chem. Phys. 35, 288 (1961).
- R. McWeeny, in "Molecular Orbitals in Chemistry, Physics, and Biology" (P.-O. Löwdin and B. Pullman, eds.), p. 305. Academic Press, New York, 1964.
- J. Kaufman and J. R. Hamann, Presented at ACS Meeting in Philadelphia, Pennsylvania, Div. of Inorganic Chemistry (1964).
- W. Giordano and P. G. Mennitt, CRDL Report 3316, Dec. 1965, Edgewood Arsenal, Maryland.